On finite-dimensional attractors of homeomorphisms (joint with Jaime Sánchez-Gabites)

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Abstract

Let E be a linear space and suppose that A is the global attractor of either (i) a homeomorphism $F: E \to E$ or (ii) a semigroup $S(\cdot)$ on E that is injective on A. In both cases A has trivial shape, and the dynamics on Acan be described by a homeomorphism $F: A \to A$ (in the second case we set F = S(t) for some t > 0). If the topological dimension of A is finite we show that for any $\epsilon > 0$ there is an embedding $e: A \to \mathbb{R}^k$, with $k \sim \dim(A)$, and a (dynamical) homeomorphism $f: \mathbb{R}^k \to \mathbb{R}^k$ such that F is conjugate to fon A (i.e. $F|_A = e^{-1} \circ f \circ e$) and f has an attractor A_f with $e(A) \subset A_f \subset$ $N(e(A), \epsilon)$. In other words, we show that the dynamics on \mathring{A} is essentially finite-dimensional.